



# Angles on Parallel lines

## Component Knowledge

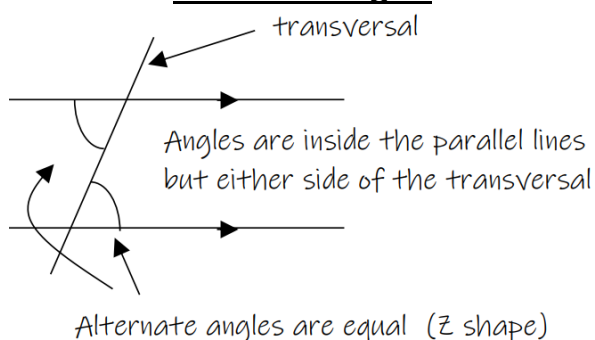
- Basic angle facts – such as angles on a straight line =  $180^\circ$
- Recognise that a transversal is a line which crosses a set of parallel lines
- To be able to find missing angles on parallel lines.

## Key Vocabulary

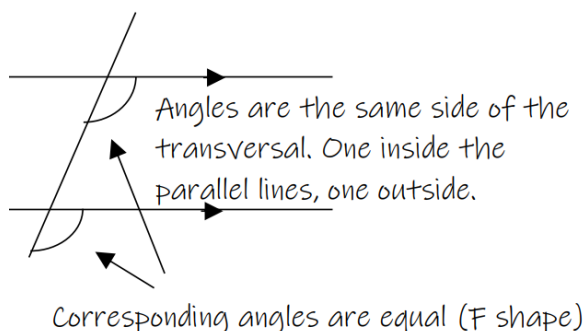
|                |                                                                                                           |
|----------------|-----------------------------------------------------------------------------------------------------------|
| Parallel lines | Lines are parallel if they are always the same distance apart (called "equidistant"), and will never meet |
| Supplementary  | Two angles are supplementary when they add up to $180^\circ$                                              |

## Parallel Lines Angle Facts:

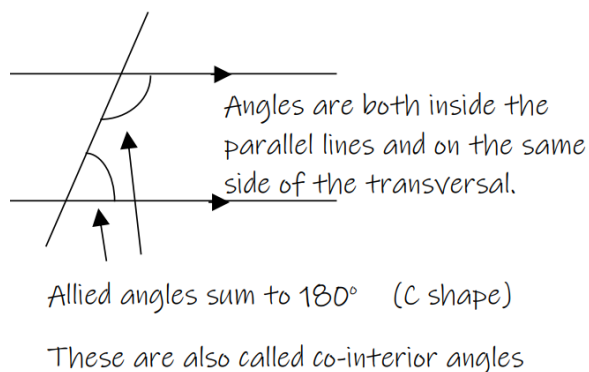
### Alternate Angles



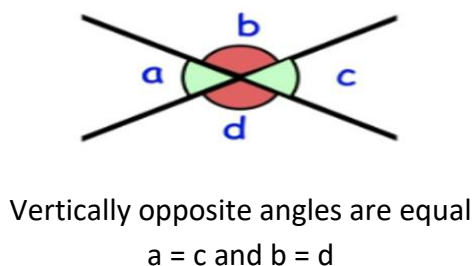
### Corresponding angles



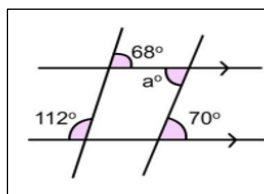
### Co-Interior Angles



### Vertically opposite angles



## Examples



$$a = 70^\circ$$

Reason -Alternate Angles are equal

Important! ALWAYS state the angle and the reason.

## Online Clips

U390, U730, U628, U732, U655, U826



# Bearings

## Component Knowledge

- To be able to understand the 3 rules of bearings and use this to measure and draw bearings.
- To be able to use angle facts to find missing bearings.

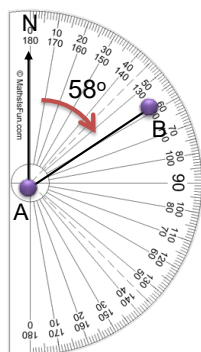
## Key Vocabulary

|            |                                                                                                                                                                                            |
|------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Bearing    | A measure of direction, it is used to represent the direction of one point relative to another. It is the angle in degrees measured clockwise from north. Always written in three-figures. |
| Protractor | The instrument used for measuring angles (measured in degrees).                                                                                                                            |
| Scale      | Used to reduce real world dimensions to a useable size.                                                                                                                                    |

Measuring and drawing Bearings using a protractor:

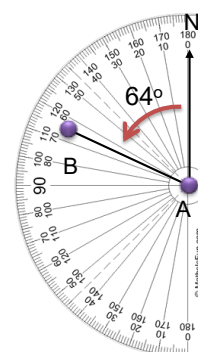
Bearings are measured and drawn

- From the **North (N)**
- clockwise**
- are always written as **3 figures**.



Bearing = 058°

To measure a bearing greater than 180°, measure the angle anticlockwise and subtract from 360°.



Bearing =  $360^\circ - 64^\circ = 296^\circ$

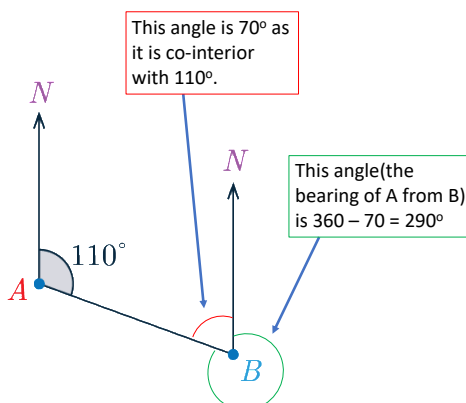
Be careful where a bearing is being measured from. If you were measuring the bearing of B from A your protractor would be on A.

Example: Bearings without a protractor

We are given the bearing of B from A. To calculate the area of A from B we can use angle facts.

Co-interior angles add up to 180°.

Angles at a point equal 360°.



Online clips

U525, U107

# Plans and elevations

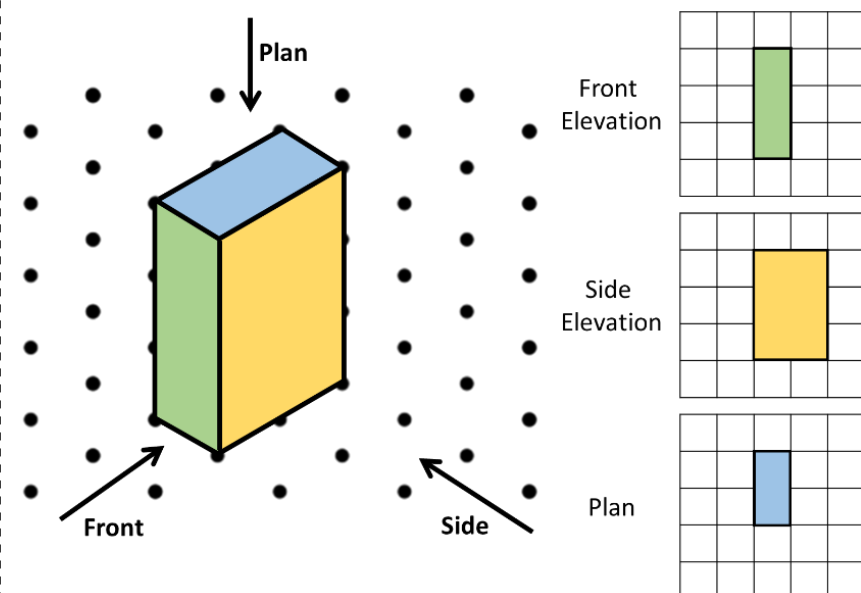


## Component Knowledge

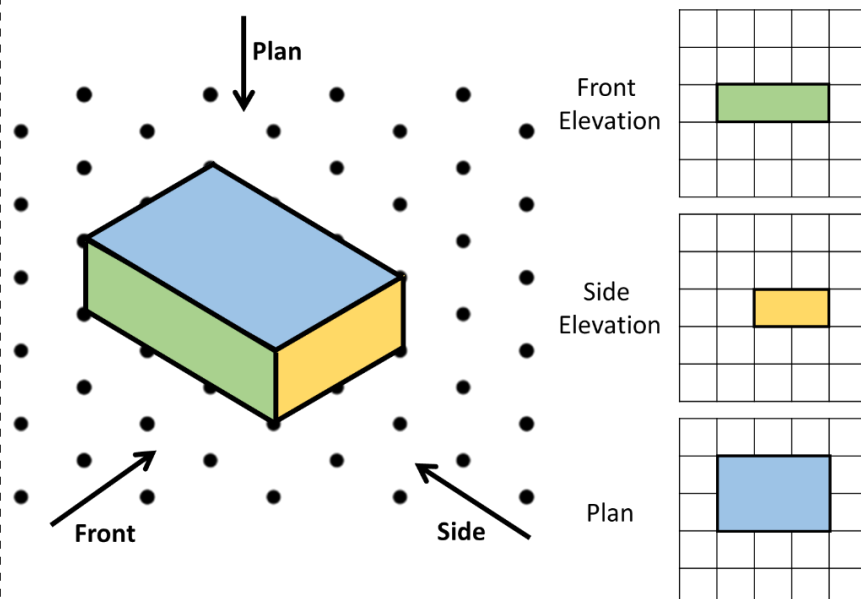
- Draw the plan of an oriented 3-dimensional shape
- Draw the front elevation (direction specified) of a 3-dimensional shape
- Draw the side elevation (direction specified) of a 3-dimensional shape

## Key Vocabulary

|                 |                                                                              |
|-----------------|------------------------------------------------------------------------------|
| Plan            | The view of an oriented 3-dimensional shape from above                       |
| Front elevation | The view of an oriented 3-dimensional shape from a specified front direction |
| Side elevation  | The view of an oriented 3-dimensional shape from the side                    |



Ensure that the dimensions of the plan and the elevation are consistent with the lengths of the 3-dimensional shape.

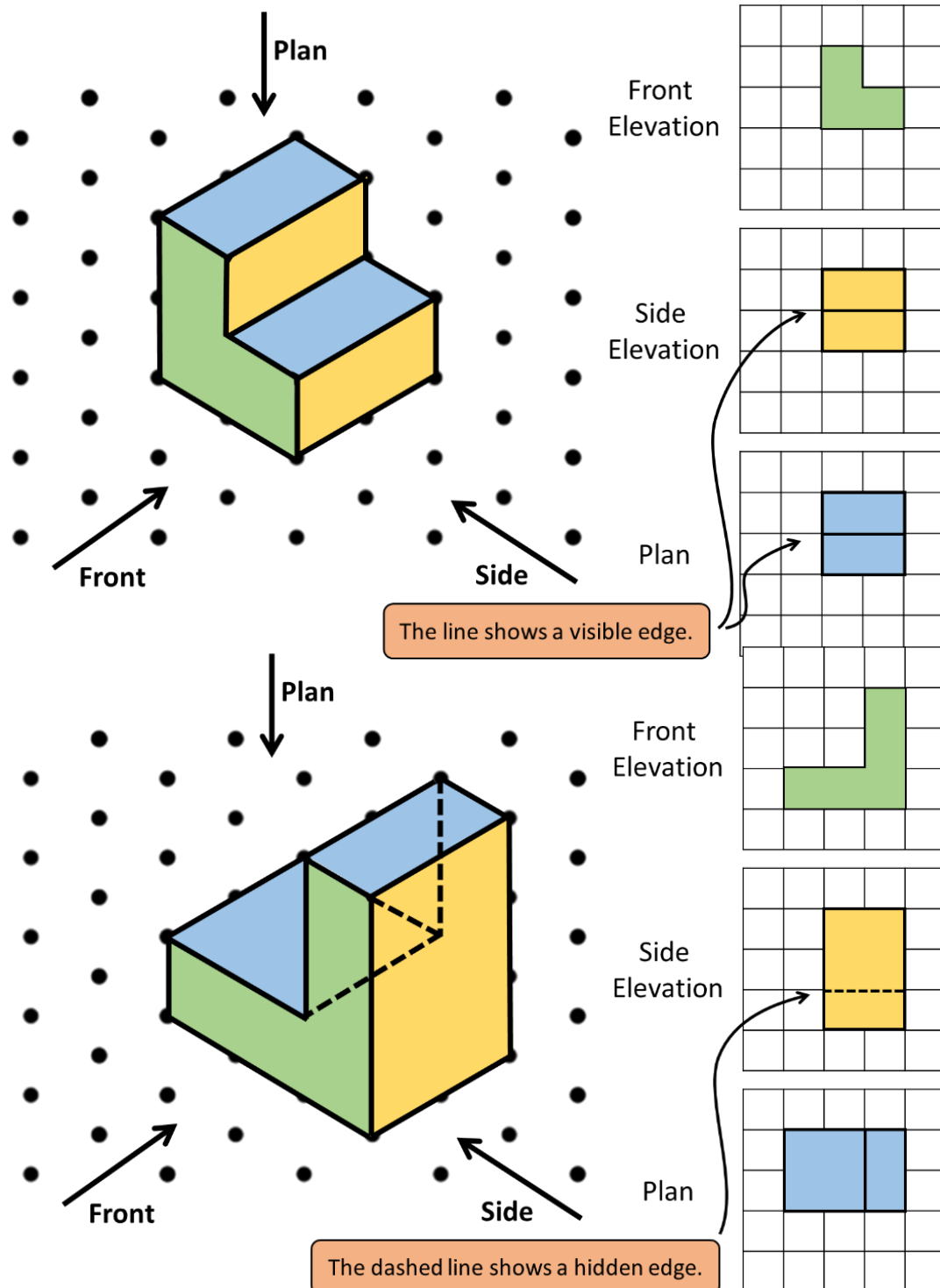


If only the front direction is specified, both the left and right-side view are acceptable as the side elevation.

(They are either the same, or mirror images)

# Showing edges in plans and elevations

This provides more information about the shapes and makes it easier to identify the direction from which the plan and elevation are drawn.





# Isometric Drawing

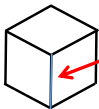
## Component Knowledge

- To be able to draw a 3D shape on Isometric paper

## Key Vocabulary

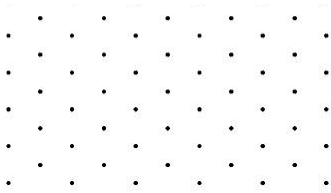
|                 |                                                                                                                                                                                            |
|-----------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Isometric       | An isometric drawing is a drawing of a 3- dimensional shape on a two- dimensional surface. A vertical line is used as a place to start. Horizontal lines are created at 30- degree angles. |
| Isometric Paper | Isometric paper is paper with dots arranged in equilateral triangles.                                                                                                                      |
| Edge            | An edge is where two faces, on a shape, come together. On 3D shapes they are the lines that separate each face.                                                                            |
| Vertex          | A vertex is a corner where edges meet.                                                                                                                                                     |
| Faces           | A face is a flat or curved surface on a 3D shape.                                                                                                                                          |

We can draw 2D representations of 3D shapes from two different angles:



This one has a front **edge**

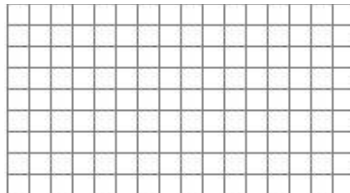
We can draw cubes from this angle on isometric paper (spotty triangle paper)



This one has a front **face**



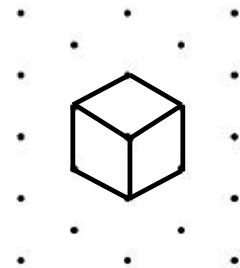
We can draw cubes from this angle on square paper.



To draw a single cube on the isometric paper.

Make sure you have the paper this way with the dots going down, not across

The lines can never be drawn horizontally.

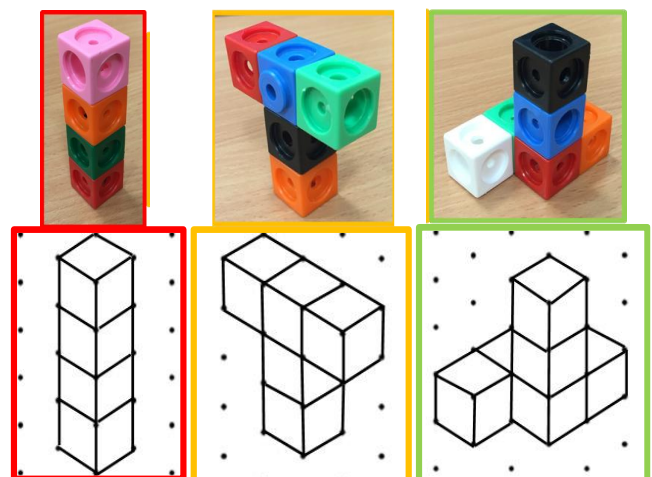
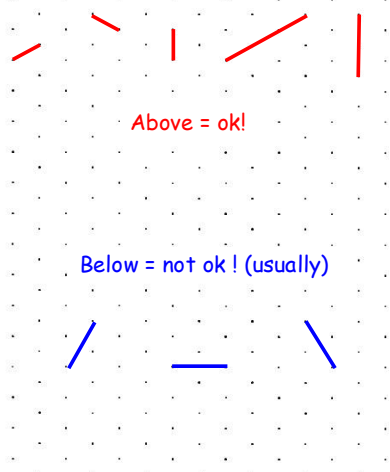


Start by drawing just one face

Then complete the cube

When drawing objects on isometric paper, you very rarely (if ever) join dots across wider gaps

They usually join to dots directly next to them...



# Straight line



## graphs

### Component Knowledge

- Recognise and sketch horizontal and vertical graphs
- Complete a table of values
- Plot straight line graphs
- Identify gradients/intercepts from a graph
- Identify gradients/intercepts from an equation

### Key Vocabulary

|             |                                                                        |
|-------------|------------------------------------------------------------------------|
| Axis        | A fixed reference line a grid to help show the position of coordinates |
| Gradient    | How steep a graph is at any point                                      |
| Y intercept | Where the graph cuts through the y axis                                |
| Coordinate  | A set of values that show an exact position                            |
| Quadrant    | Any of the 4 areas made when we divide up a plane by an x and y axis   |
| Vertical    | In an up and down position. The y axis is the vertical axis            |
| Horizontal  | Going side to side. The x axis is the horizontal axis                  |
| Graph       | A diagram showing the relationship between two quantities              |

### Completing a table of values and plotting a graph

To plot a straight line graph, you may be given a table or you may need to draw one.

Example: Plot the graph of  $y = 4x - 2$  for the values of  $x$  from -3 to 3.

1) Draw a table of values if you have not been given one.

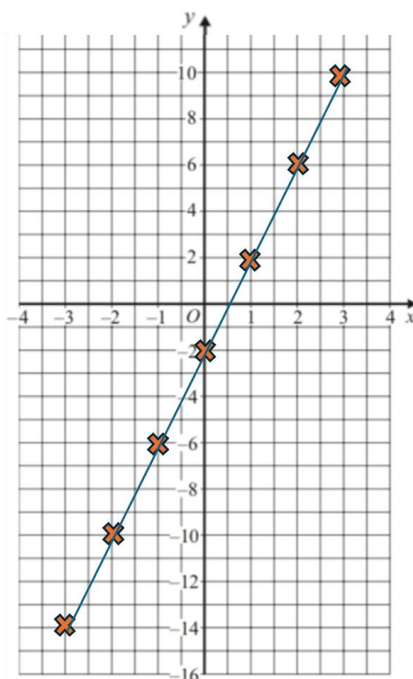
|   |    |    |    |   |   |   |   |
|---|----|----|----|---|---|---|---|
| x | -3 | -2 | -1 | 0 | 1 | 2 | 3 |
| y |    |    |    |   |   |   |   |

2) Substitute in your  $x$  values to  $y = 4x - 2$ , this will give the corresponding  $y$  values.

|   |     |     |    |    |   |   |    |
|---|-----|-----|----|----|---|---|----|
| x | -3  | -2  | -1 | 0  | 1 | 2 | 3  |
| y | -14 | -10 | -6 | -2 | 2 | 6 | 10 |

3) Plot the points on the graph.

E.g. (-3, -14), (-2, -10), (-1, -6), (0, -2), .... etc



4) Join up with a straight line.

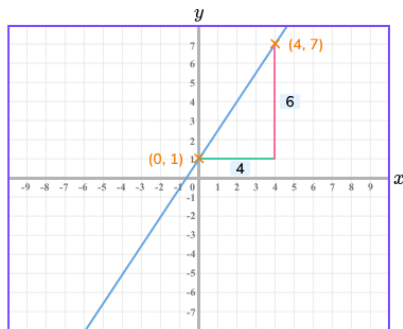
The equations of all straight lines can be written in the form:

$$y = mx + c$$

Gradient – The number in front of the x.  
This tells us how steep the line is.

Intercept – The number on its own.  
Shows where the line cuts the y axis.

The gradient of a line tells us how steep the line is,  
the greater the gradient the steeper the line.



You can find the gradient using the graph by picking 2 points on the line and using

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

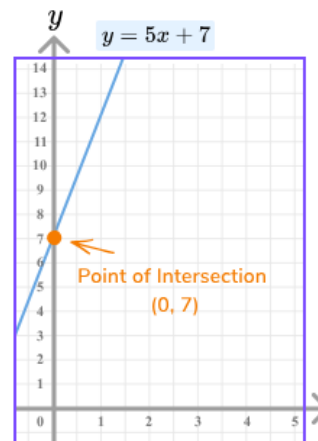
The change in y is equal to  $y_2 - y_1 = 7 - 1 = 6$

The change in x is equal to  $x_2 - x_1 = 4 - 0 = 4$

$$m = \frac{6}{4}$$

The y intercept is where the line crosses the y axis

You can find the y intercept from the equation by putting x equal to 0



The gradient and intercept of a straight line can also be identified from the formula.

Example: Find the gradient and intercept of the following lines.

1)  $y = 5x - 2$

Grad = 5 Intercept = - 2

2)  $2y = 4x + 5$

$y = 2x + 2.5$

Grad = 2 Intercept = 2.5

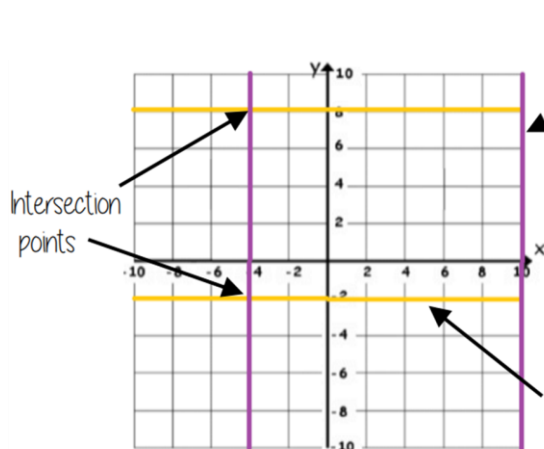
3)  $x + y = 10$

$y = -x + 10$

Grad = - 1 Intercept = 10

Rearrange all equations so they are in the form  $y = mx + c$  (the y must be isolated)

### Lines parallel to the axis (Horizontal and Vertical lines)



Lines parallel to the **y** axis take the form  **$x = a$**  and are **vertical**

Lines parallel to the **x** axis take the form  **$y = a$**  and are **horizontal**

All the points on this line have a y coordinate of -2

e.g. (3, -2) (7, -2) (-2, -2) all lay on this line because the y coordinate is -2

### Online clips

M797, M932, M544, M888



# Approximate Solutions to Equations Using Graphs

## Component Knowledge

- Be able to draw straight line graphs.
- Be able to approximate solutions from graphs.

## Key Vocabulary

|              |                                                                            |
|--------------|----------------------------------------------------------------------------|
| Graph        | A diagram showing the relationship between two quantities                  |
| Equation     | A mathematical statement showing that two expressions are equal            |
| Approximate  | Close to an actual value but may not be completely accurate                |
| Solution     | Values for which an equation is true                                       |
| Linear       | Increasing or decreasing at a constant rate to form a straight line        |
| Co-Ordinates | A pair of numbers used to describe the position of a point                 |
| Axis/Axes    | A fixed reference line on a grid to help show the position of co-ordinates |
| Plot         | To represent the relationship between two quantities graphically           |
| Simultaneous | When two or more things occur at the same time                             |
| Intersect    | When two or more things pass through each other                            |

Equations describe a relationship between two values. We can plot this relationship on a graph to help us visualise the relationship more easily. By doing this we can also approximate solutions for given equations.

The equations of all straight lines can be written in the form:

$$y = mx + c$$

Gradient – The number in front of the  $x$ .  
This tells us how steep the line is.

Intercept – The number on its own.  
Shows where the line cuts the  $y$  axis.

## Plotting Linear Graphs

Draw the graph of:  $y = 2x + 1$

|     |    |   |   |   |   |
|-----|----|---|---|---|---|
| $x$ | -1 | 0 | 1 | 2 | 3 |
| $y$ | -1 | 1 | 3 | 5 | 7 |

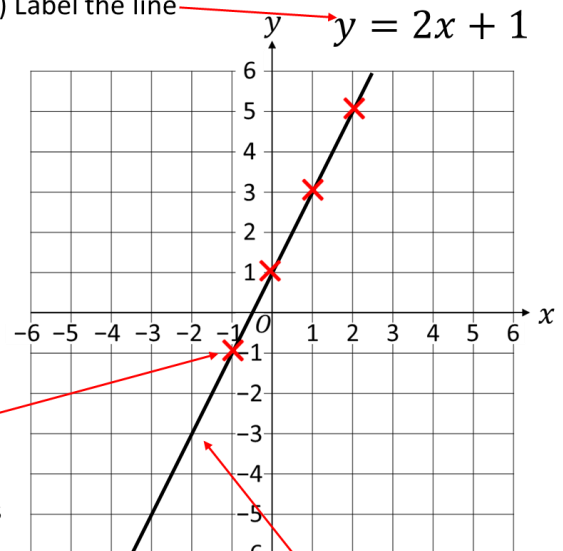
$(-1, -1)$   $(0, 1)$   $(1, 3)$   $(2, 5)$   $(3, 7)$

E.g.  $(2 \times 2) + 1 = 5$

1) Complete the table of values by substituting  $x$  values.

2) Plot each pair of values as coordinates.

4) Label the line  $y = 2x + 1$

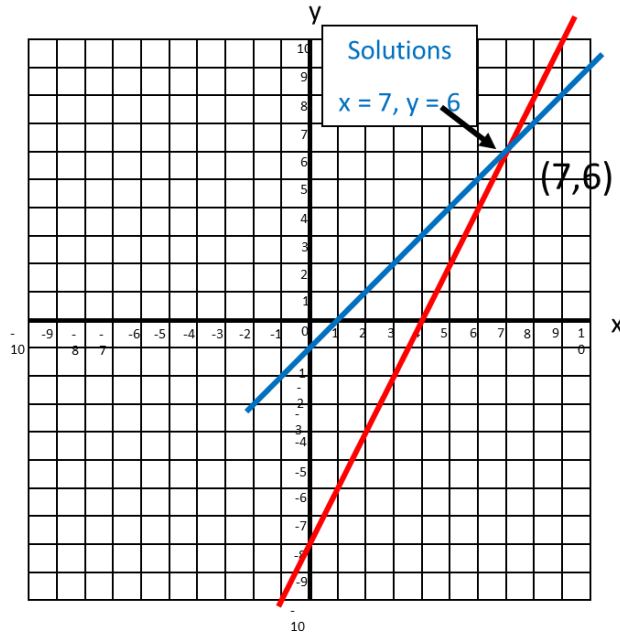


3) Join the points to make a line.

## Solving Simultaneous Equations When the Graph is Given

Solve the simultaneous equations

$$2x - y = 8 \text{ and } x - y = 1$$



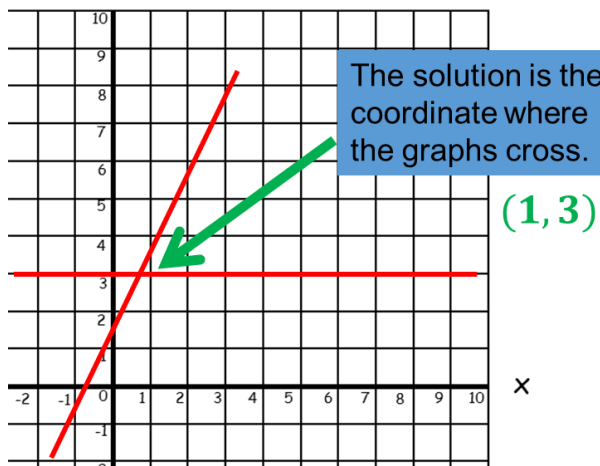
The solution to the simultaneous equation is where the two lines intersect.

There will always be two solutions one for x and one for y.

So  $x = 7$  and  $y = 6$ .

## Plotting and Solving Graphically

Solve the simultaneous equations  $y = 2x + 1$  and  $y = 3$  graphically:



Sometimes we are asked to show the solution graphically but not given the graphs.

In these cases we must first plot the graphs as shown previously.

First sketch  $y = 3$ .

Draw a table of values to sketch  $y = 2x + 1$  and plot the line

| x | 0 | 1 | 1 |
|---|---|---|---|
| y | 1 | 3 | 5 |

So  $x = 1$  and  $y = 3$ .

Online clips

U836

# Simultaneous linear equations



## Component Knowledge

- Solving simultaneous linear equations with a balanced variable by elimination
- Solving simultaneous linear equations where balancing a variable is required
- Form and solve simultaneous equations.

## Key Vocabulary

|                        |                                                                                                                                           |
|------------------------|-------------------------------------------------------------------------------------------------------------------------------------------|
| Simultaneous equations | Two or more equations that are to be solved (if possible) by using the <i>same</i> value for each variable                                |
| Coefficient            | The number factor in an algebraic term, multiplied with variables (e.g. 4 in $4x$ )                                                       |
| Balancing variables    | Equating the coefficients of like terms in different equations by multiplying with suitable factors                                       |
| Eliminating variables  | Reducing the term containing a particular variable in an equation to 0 by subtracting/adding another equation with the same/opposite term |
| Substitution           | Assigning a value to a variable (e.g. substituting $y = 8$ in $6y$ gives 48)                                                              |

## Solving simultaneous equations – no balancing needed

In the first example, because the two equations have **equal** terms in  $x$  – both are  $3x$  – *subtracting* the equations (remember to subtract both sides) *eliminates* the  $x$  term. The resulting equation has only one unknown,  $y$ , and can be solved.

Here the value found for  $y$  is **substituted** into the second equation to obtain an equation in terms of  $x$ . The first equation could have been used too.

Whichever equation is used for substitution, it is good practice to check the pair of values found in the other equation too, to ensure no mistakes have been made:

$$3 \times 3 + 2 \times 5 = 19$$

In the second example, because the two equations have **opposite** terms in  $y$  – one is  $2y$  and the other  $-2y$  – *adding* the equations eliminates the  $y$  term.

$$\begin{array}{r} 3x + 4y = 29 \\ \dots \\ - 3x + 2y = 19 \\ \hline \end{array}$$

$$\begin{array}{r} 2y = 10 \\ y = 5 \end{array}$$

Substitute  $y$  into either equation to find  $x$ .

$$\begin{array}{r} 3x + (2 \times 5) = 19 \\ 3x + 10 = 19 \\ 3x = 9 \\ x = 3 \end{array}$$

$$\begin{array}{r} 3x + 2y = 16 \\ \dots \\ + 2x - 2y = 4 \\ \hline 5x = 20 \\ x = 4 \end{array}$$

Substitute  $x$  back in to find  $y$ .

$$\begin{array}{r} (2 \times 4) - 2y = 4 \\ 8 - 2y = 4 \\ 8 = 4 + 2y \\ 4 = 2y \\ 2 = y \end{array}$$

## Forming simultaneous equations – balancing a variable

$$\begin{array}{rcl}
 2x + 8y & = & 32 \\
 x + 3y & = & 13 \quad \times 2 \\
 \hline
 2x + 6y & = & 26 \quad \star \\
 \hline
 2y & = & 6 \\
 y & = & 3 \\
 \\ 
 2x + 6(3) & = & 26 \\
 2x + 18 & = & 26 \\
 2x & = & 8 \\
 x & = & 4
 \end{array}$$

Here neither the  $x$  nor the  $y$  terms are already balanced. But the  $x$  terms can be balanced by multiplying the second equation by 2. (Remember to **multiply both sides** by the factor.)

The modified second equation can then be subtracted from the first, and the subsequent steps are as before.

$$\begin{array}{rcl}
 5x + 4y & = & 19 \\
 2x - 3y & = & 3 \quad \times 4 \\
 \hline
 8x - 12y & = & 12 \quad \times 3 \\
 \hline
 15x + 12y & = & 57 \\
 \hline
 23x & = & 69 \\
 \\ 
 x & = & 3 \\
 \\ 
 15 + 4y & = & 19 \\
 4y & = & 4 \\
 y & = & 1
 \end{array}$$

In this example the  $y$  terms can be balanced by multiplying the first equation by 3 and the second by 4, since 12 is the lowest common multiple of the starting coefficients. (Alternatively, we can balance the  $x$  terms. What factors would be needed in that case?)

The modified equations are then added – since the  $y$  terms have opposite signs – and the following steps are as before.

## Forming simultaneous equations to solve a problem

*Barry buys 200 pieces of stationery for £76.*

*Of the 200 pieces of stationery,  $x$  of them are rulers that cost 50p each and  $y$  of them are pens that cost 20p each.*

*Find how many rulers and pens Barry buys.*

The information in the question can be written as the simultaneous equations

$$x + y = 200$$

$$50x + 20y = 7600 \text{ (amounts are written in pence)}$$

Multiply the first equation by 50 to give  $50x + 50y = 10000$ . The  $x$  terms are now balanced, and subtracting the second equation gives  $30y = 2400$ .

Therefore  $y = 80$ , and using the first equation  $x = 120$ .

Online clips

U760

# Congruency



## Component Knowledge

- Know what congruency is and how to identify whether shapes are congruent
- Recognise congruent triangles
- Know the rules for congruency

## Key Vocabulary

|             |                                                              |
|-------------|--------------------------------------------------------------|
| Congruent   | The same shape and size                                      |
| Triangle    | A 3 sided flat shape with straight sides                     |
| Hypotenuse  | The side opposite the right angle in a right angles triangle |
| Right angle | An angle which is equal to $90^\circ$                        |
| Identical   | Exactly the same                                             |
| Side        | One of the line segments that make a flat 2D shape           |

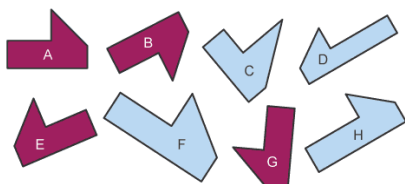
## Key Concepts

Shapes are **congruent** if they are **identical** – same shape and same size.

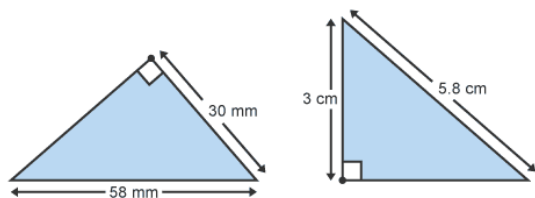
Shapes can be rotated or reflected but still be congruent.

## Examples

Which shapes are congruent?



Shapes A, B, E and G are congruent as they are identical in size and shape.



These are congruent, they both have a right angle, the same hypotenuse and another side the same

## Triangles

There are four ways of proving that two triangles are congruent:

- 1) **SSS** (Side, Side, Side)
  - a. All 3 sides are the same in both triangles
- 2) **RHS** (Right angle, Hypotenuse, Side)
  - a. Both triangles have a right angle, the same hypotenuse and one other side the same
- 3) **SAS** (Side, Angle, Side)
  - a. Two sides with the angle in between them are the same in both triangles
- 4) **ASA** (Angle, side, Angle) or **AAS**
  - a. One side and two angles are the same in both triangles

## Misconceptions

Proving all 3 angles are the same is **not** proving they are congruent, as one could be an enlargement of the other.

Angle, Side, Side is **not** a proof for congruency as the angle needs to be contained between the two sides.

## Online clips

U790, U112, U866

# Similar shapes



## Component Knowledge

- Identify similar shapes
- Work out missing sides and angles in similar shapes
- Use parallel lines to find missing angles in similar shapes
- Understand similarity & congruence

## Key Vocabulary

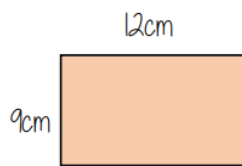
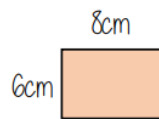
|               |                                                                                              |
|---------------|----------------------------------------------------------------------------------------------|
| Enlarge       | Make a shape bigger (or smaller) by a given multiplier (scale factor)                        |
| Scale factor  | The multiplier of enlargement                                                                |
| Similar       | When one shape can become another through a reflection, rotation, enlargement or translation |
| Corresponding | Items that appear in the same place in two similar situations                                |

## Identifying similar shapes



Angles in similar shapes do not change.  
e.g. if a triangle gets bigger the angles can not go above  $180^\circ$

Similar shapes



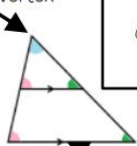
Scale Factor:  
Both sides on the bigger shape are 1.5 times bigger

Compare sides:  $6:9$   $8:12$   
 $2:3$   $2:3$

Both sets of sides are in the same ratio

## Similar triangles

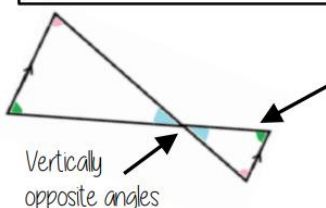
Shares a vertex



Because corresponding angles are equal the highlighted angles are the same size

Parallel lines — all angles will be the same in both triangle

As all angles are the same this is similar — it only one pair of sides are needed to show equality

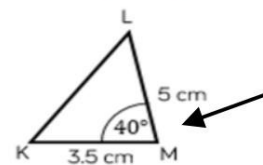
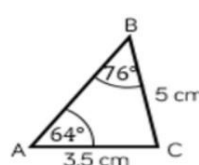


Vertically opposite angles

All the angles in both triangles are the same and so similar

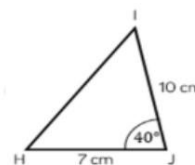
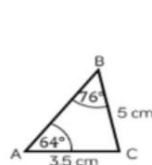
## Congruence & similarity

Congruent shapes are identical — all corresponding sides and angles are the same size



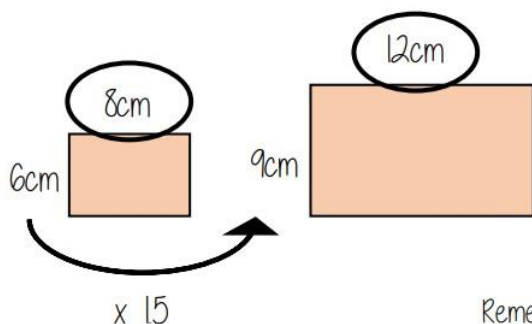
$\angle C = \angle M$

Because all the angles are the same and  $AC=KM$   $BC=LM$  triangles ABC and KLM are **congruent**



Because all angles are the same, but all sides are enlarged by 2  
ABC and HIJ are **similar**

## Information in similar shapes



Compare the equivalent side on both shapes

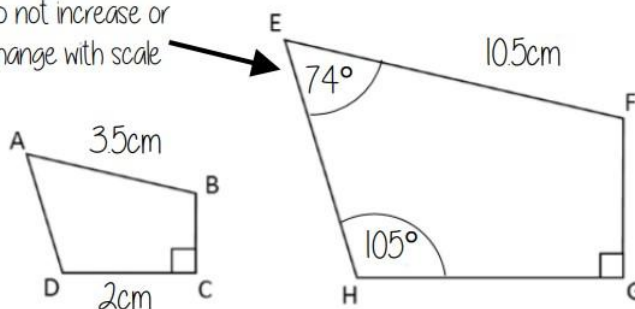
Scale Factor is the multiplicative relationship between the two lengths

Shape ABCD and EFGH are similar

Notation helps us find the corresponding sides

AB and EF are corresponding

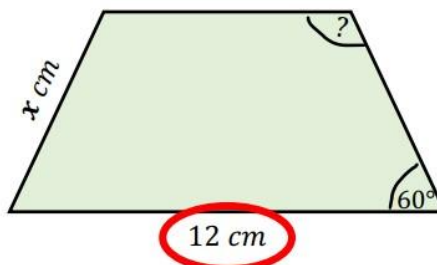
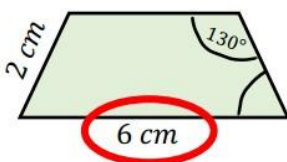
Remember angles do not increase or change with scale



## Further example

Don't forget that properties of shapes don't change with enlargements or in similar shapes

The two trapezium are similar find the missing side and angle



Corresponding sides identify the scale factor

$$\frac{12}{6} = 2$$

Scale Factor = 2

Calculate the missing side

Length (corresponding side)  $\times$  scale factor

$$2\text{cm} \times 2$$

$$x = 4\text{cm}$$

Enlargement does not change angle size

Calculate the missing angle

Corresponding angles remain the same  
 $130^\circ$

## Online clips

M124, M377, M324, M606

# Enlargement



## Component Knowledge

- Enlarge a rectilinear shape by a given positive scale factor
- Enlarge a rectilinear shape, given a positive integer scale factor and a centre
- Enlarge a rectilinear shape, given a positive fractional scale factor and a centre
- Describe an enlargement in terms of scale factor and centre

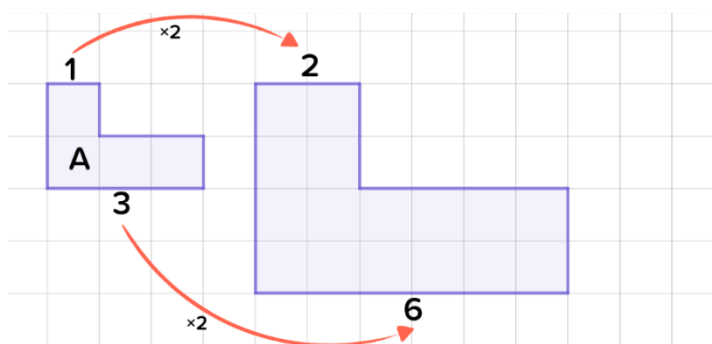
## Key Vocabulary

|                       |                                                                                                         |
|-----------------------|---------------------------------------------------------------------------------------------------------|
| Enlargement           | A transformation of a shape in which all dimensions are multiplied by the same number                   |
| Scale factor          | The number by which dimensions are multiplied in an enlargement                                         |
| Centre of enlargement | The point from which distances to the <i>object</i> and the <i>image</i> of an enlargement are measured |

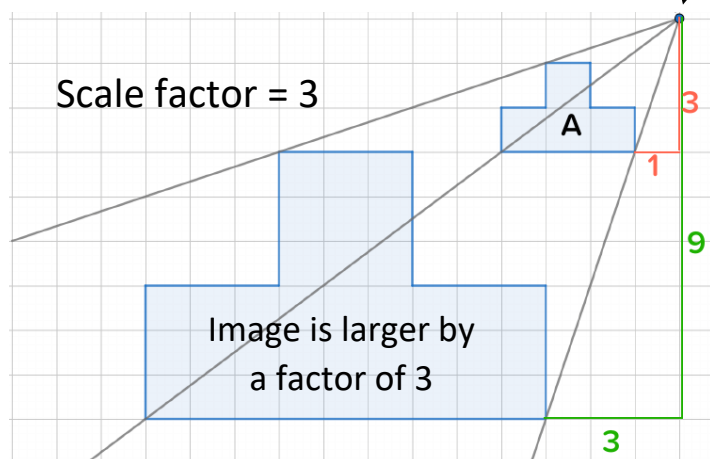
## Enlarging by a scale factor

In an *enlargement* all dimensions are multiplied by the same number, called the **scale factor**. In this example shape A has been enlarged by scale factor 2.

If the scale factor is smaller than 1 the dimensions are in fact reduced (divided), although the transformation is still called an enlargement! (See next page)

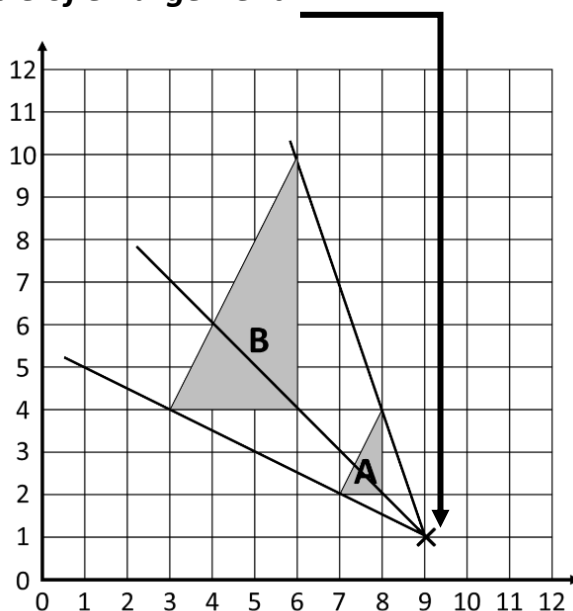


## Enlarging by a positive integer scale factor from a centre



Measure the distance from the centre of enlargement to each vertex of the *object* shape A; the corresponding vertex in the *image* is triple that distance in the **same** direction

## Centre of enlargement

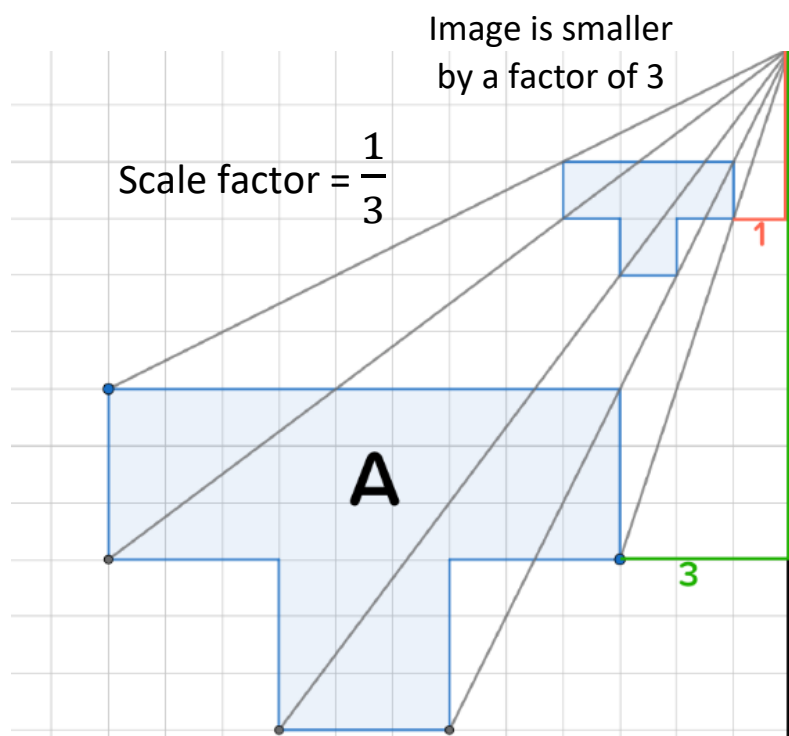


If the object shape is drawn on a coordinate grid, the centre may be specified by coordinates (here the centre is (9,1))

## Enlarging by a positive *fractional* scale factor from a centre

A positive scale factor that is smaller than 1 reduces the dimensions of the object shape.

Here the distance from the centre of enlargement to each vertex of the object shape A is measured and then **divided** by 3 to find the corresponding vertex in the image (still in the same direction)



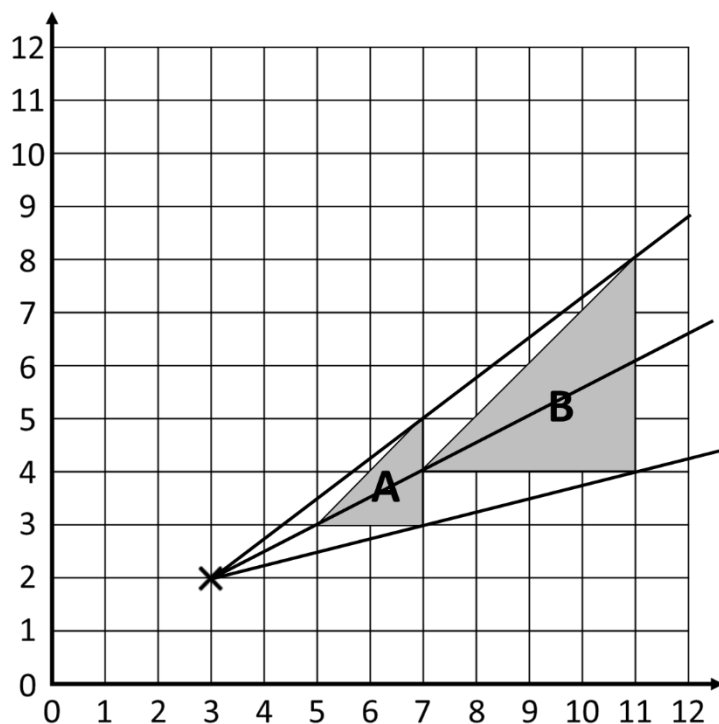
## Describing an enlargement

An enlargement is easily identified as such by the change in dimensions.

To determine the scale factor, calculate the ratio of the lengths of corresponding sides in the object and its image.

For the centre, draw lines through two pairs of corresponding vertices and find their point of intersection (thus retracing the steps of the process of enlarging)

The enlargement shown here – from A to B – has scale factor 2 and centre (3,2)



[Online clips](#)

M178, U519



# Sampling

## Component Knowledge

- Know the difference between random sampling and stratified sampling
- To know how to take a random sample
- To know how to calculate sample sizes for stratified sampling

## Key Vocabulary

|                   |                                                                                           |
|-------------------|-------------------------------------------------------------------------------------------|
| Qualitative data  | Data collected that is described in words not numbers. e.g. race, hair colour, ethnicity. |
| Quantitative data | This is the collection of numerical data that is either discrete or continuous.           |
| Population        | This is the whole group you are collecting data from.                                     |
| Sample            | A sample is part of the whole population.                                                 |

## Simple Random Sampling

A simple random sample is when each member of the population under study has the same chance or probability of being selected for the sample.

An example of a simple random sample would be:

1. Assign a number to every member of the population
2. Randomly generate numbers using numbers from a hat or a computer calculator
3. Use the data from the corresponding members of the population

The following options are not random as not everyone has the same chance of being chosen:

- Choose the first 50 people who arrive at the office.
- Choose 50 people whose surname begins with J or T.
- List all the office workers in alphabetical order and choose every 5th name on the list.

## Systematic sampling

- This is a very similar method to random sampling, but the population would first be ordered according to specific criteria such as listing names of people in the population in alphabetical order.
- The sample would be drawn by selecting every nth person. For example, every 10th person in the list.

## Online clip

U162

A sample should be:

- fair and unbiased
- large enough in size to be representative of the whole population under study.

## Stratified Sampling

A stratified sample involves grouping members of the population into classes before taking a proportionate sample from each class (e.g. grouped by age, language etc.)

To find the amount of people in each class we must do the following calculation  $\frac{\text{Class size}}{\text{total population}} \times \text{sample size}$

### Example

The table below shows the age group of the members of a tennis club.

|           |        |       |        |
|-----------|--------|-------|--------|
| Age Group | Junior | Adult | Senior |
| Number    | 320    | 500   | 130    |

Total population=

$$320 + 500 + 130 = 950$$

A stratified sample of 40 is to be taken. Calculate the number for each age group in the sample.

### Junior

$$\frac{320}{950} \times 40 = 13.5 \approx 14 \text{ people}$$

### Adult

$$\frac{500}{950} \times 40 = 21.1 \approx 21 \text{ people}$$

### Senior

$$\frac{130}{950} \times 40 = 5.4 \approx 5 \text{ people}$$



# Averages from a frequency table

## Component Knowledge

- To be able to calculate the mean, median, mode and range from a frequency table.

## Key Vocabulary

|           |                                                                                              |
|-----------|----------------------------------------------------------------------------------------------|
| Frequency | The number of pieces of data we have.                                                        |
| Mean      | Add up the values you are given and divide by the number of values you have.                 |
| Median    | The middle value when the data is in order.                                                  |
| Mode      | The value or item with the highest frequency.                                                |
| Range     | This is the difference between the largest and smallest values. Shows the spread of the data |

A team played 10 games and recorded the number of goals scored in those games.

| Goal scored ( $x$ ) | Frequency ( $f$ ) | Total Frequency so far | $(fx)$ ( $f$ multiplied by $x$ ) |
|---------------------|-------------------|------------------------|----------------------------------|
| 0                   | 2                 | (2) 2                  | $0 \times 2 = 0$                 |
| 1                   | 2                 | (2+2) 4                | $1 \times 2 = 2$                 |
| 2                   | 5                 | (2+2+5) 9              | $2 \times 5 = 10$                |
| 3                   | 1                 | (2+2+5+1) 10           | $3 \times 1 = 3$                 |
| Total               | 10                |                        | 15                               |

### Calculating the mean number of goals scored.

Step 1: calculate the total frequency

Step 2: calculate  $(fx)$

Step 3: calculate the mean using the formula  $\frac{\text{total } fx}{\text{total frequency}}$

$$\text{Mean} = \frac{15}{10} = 1.5 \text{ goals}$$

### Calculating the mode number of goals scored.

Mode = highest frequency of goals scored

Highest frequency = 5 for 2 goals scored

Mode = 2 goals scored

### Calculating the median number of goals scored.

$$\text{Median value} = \frac{\text{Total frequency} + 1}{2}$$

$$\frac{11}{2} = 5.5^{\text{th}} \text{ value}$$

Median = 2 goals

add the frequency column until you reach the value in-between the 5<sup>th</sup> and 6<sup>th</sup> value

### Calculating the range number of goals scored.

Highest number of goals = 3

Lowest number of goals = 0

Range = 3 - 0

Range = 3

# Averages from a grouped frequency table



## Component Knowledge

- Calculate an estimate for the mean from a grouped frequency table.
- Calculate the modal class interval from a grouped frequency table.
- Calculate the median from a grouped frequency table.

## Key Vocabulary

|                |                                                                                                                       |
|----------------|-----------------------------------------------------------------------------------------------------------------------|
| Average        | A number expressing the central or typical value in a set of data, particularly the mode, median or mean.             |
| Grouped Data   | If we have a large spread of data, we put it into categories (classes) to make the data easier to display or analyse. |
| Class interval | Group.                                                                                                                |

## Averages from grouped data

a) Find an estimate for the mean of this data.

| Length<br>(L cm) | Frequency<br>(f) | Midpoint<br>(x) | $fx$                 |
|------------------|------------------|-----------------|----------------------|
| $0 < L \leq 10$  | 10               | 5               | $10 \times 5 = 50$   |
| $10 < L \leq 20$ | 15               | 15              | $15 \times 15 = 225$ |
| $20 < L \leq 30$ | 23               | 25              | $23 \times 25 = 575$ |
| $30 < L \leq 40$ | 7                | 35              | $7 \times 35 = 245$  |
| Total            | 55               |                 | 1095                 |

Step 1: Calculate the total frequency.

Step 2: Find the midpoint of each group.

Step 3: frequency ( $f$ ) x midpoint ( $x$ ).

Step 4: Calculate the estimated mean.

$$\frac{\text{Total } fx}{\text{Total } f} = \frac{1095}{55} = 19.9\text{cm}$$

b) Identify the modal class interval.

Modal class is  $20 < L \leq 30$

Modal Class = The group that has the highest frequency.

c) Identify the group in which the median would lie.

$$= \frac{56}{2} = 28^{\text{th}} \text{ Value.}$$

$$\text{Median Value} = \frac{\text{Total frequency} + 1}{2}$$

Add the frequency column until you reach the 28<sup>th</sup> value.

Median is in the group  $20 < L \leq 30$

## NOTE:

For grouped data, we can only calculate an estimate for each average as we do not know the exact values in each group.

## Online clip

M287